

# Inductive Invariants for Noninterference in Multi-Agent Workflows

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July 11, 2018



# Section 1

## Setting

# Motivation

Conference Management (EasyChair, HotCRP, ...)  
Used by authors, reviewers, PC chair, ...

The logo for HotCRP.com, featuring the text "HotCRP.com" in a bold, red, sans-serif font. The text is centered within a light red rectangular background that has a darker red horizontal bar at the bottom.

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**2.60** 19.Jul.2013

Major new feature: Paper managers. Administrators can assign PC members to "manage" individual papers. These PC members gain admin rights over those papers, and can, for example, assign reviewers as usual.

This required extensive rearchitecting of system internals to (hopefully) avoid information leaks.

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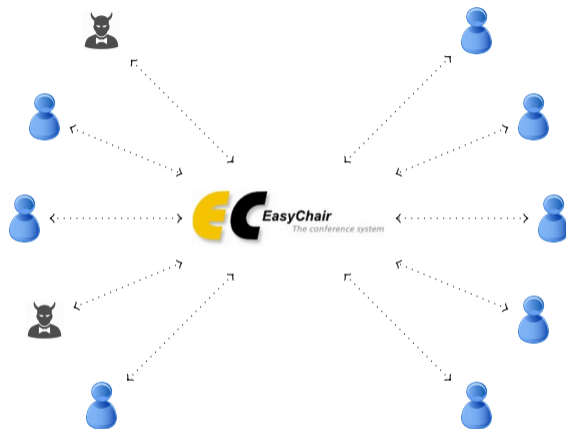
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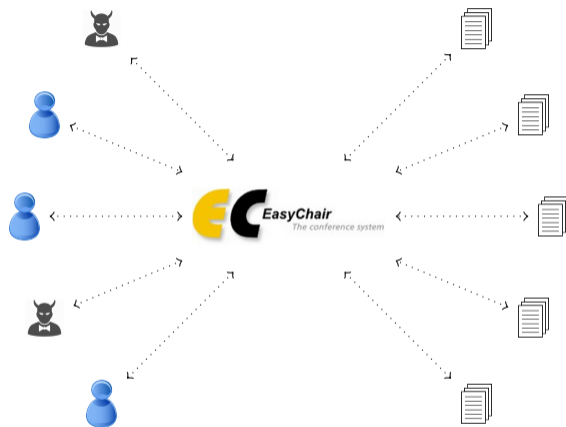
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Systems need to protect sensitive information!

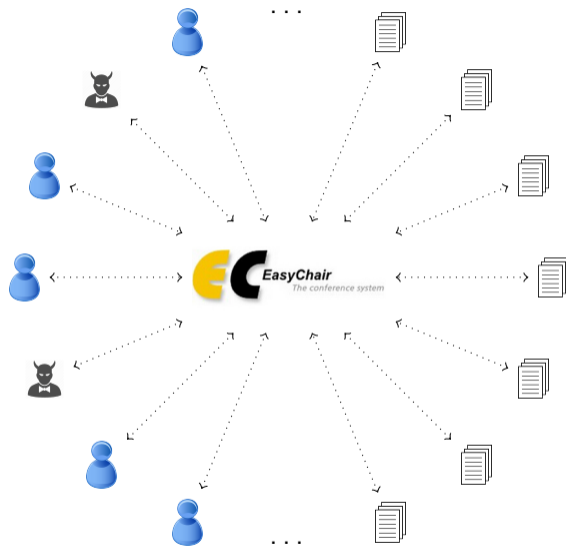
# Challenges



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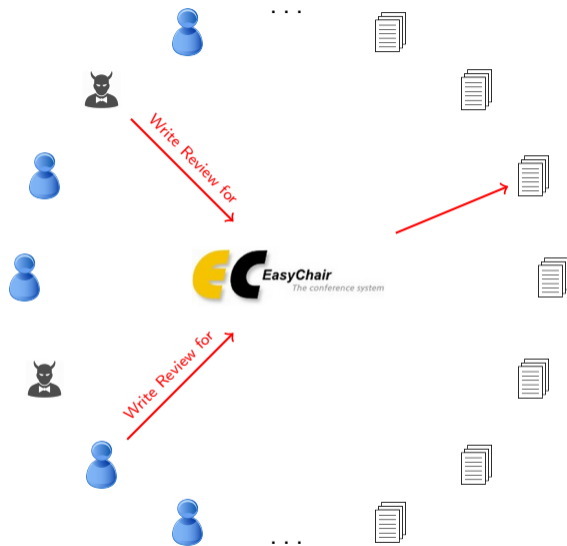


# Challenges





# Challenges



## Conflict Declaration

PC Members may declare conflicts of interest with papers.

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Reviewers

Papers

*H. Seidl* 

 *Common Opening Strategies*

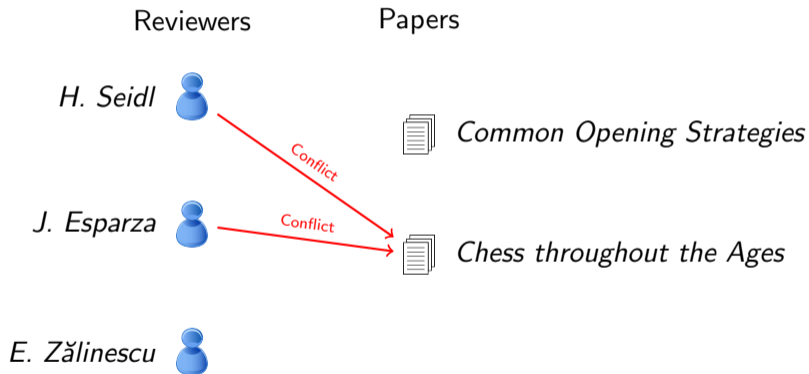
*J. Esparza* 

 *Chess throughout the Ages*

*E. Zălinescu* 

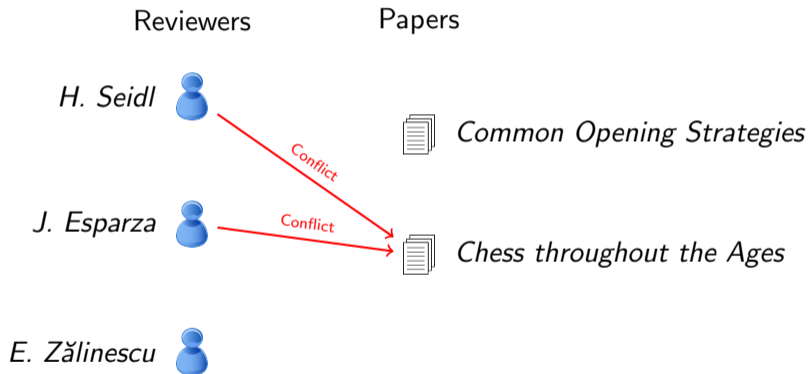
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**forall**  $x: PCMember, p: Paper. \text{ may } true \rightarrow Conflict += (x, p)$

# Complete Example Workflow

*% 1. PC members may declare conflicts*

*% 2. PC members are assigned to papers*

*% 3. PC members write reviews for papers*

*% 4. PC members read all reviews*

*% 5. PC members can update their reviews*

# Complete Example Workflow

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*% 3. PC members write reviews for papers*

**forall**  $x: PCMember, p: Paper, r: Review$ .

$Assign(x, p) \wedge Oracle(x, p, r) \rightarrow Review += (x, p, r)$

**loop** {

*% 4. PC members read all reviews*

**forall**  $x: PCMember, y: PCMember, p: Paper, r: Review$ . **may**

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*% 5. PC members can update their reviews*

**forall**  $x: PCMember, p: Paper, r: Review$  **may**.

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## Semantics of the Workflow in *Sorted First Order Logic*

**forall**  $x: PCMember, y: PCMember, p: Paper, r: Review$ . **may**  
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# Noninterference

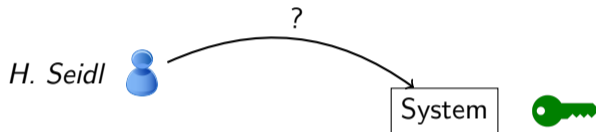
Can any agent learn secret information?

*H. Seidl* 

System 

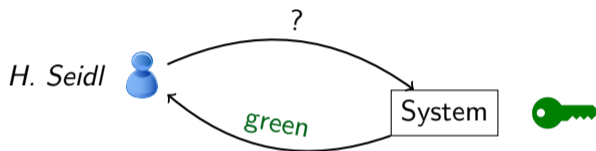
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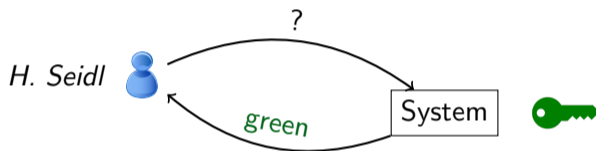
# Noninterference

Can any agent learn secret information?



# Noninterference

Can any agent learn secret information?



Does *H. Seidl* learn something?



# Noninterference — Hyperproperty

*H. Seidl* 

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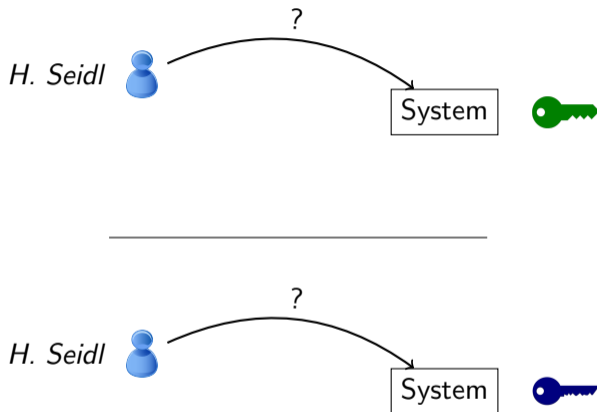
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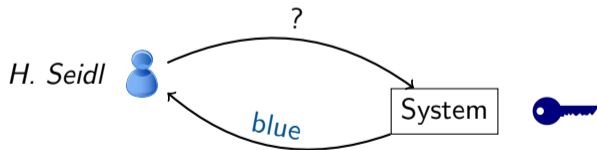
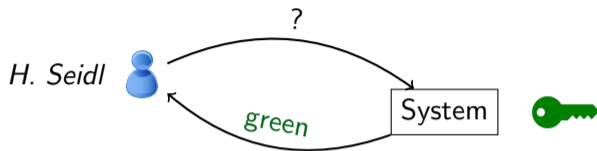
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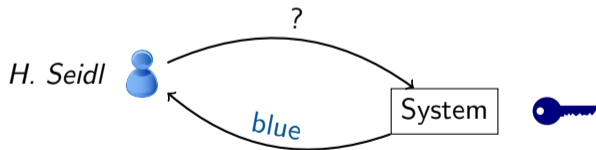
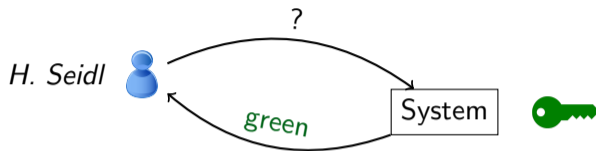
# Noninterference — Hyperproperty



# Noninterference — Hyperproperty



## Noninterference — Hyperproperty




Is this enough?

# Noninterference

*H. Seidl* 

System



*J. Esparza* 

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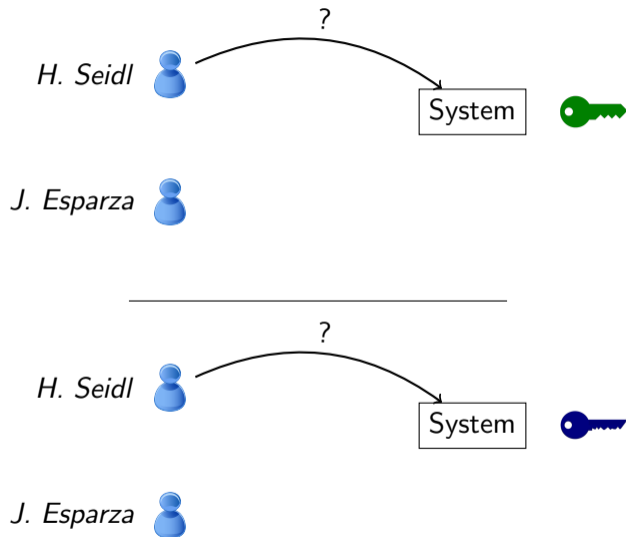
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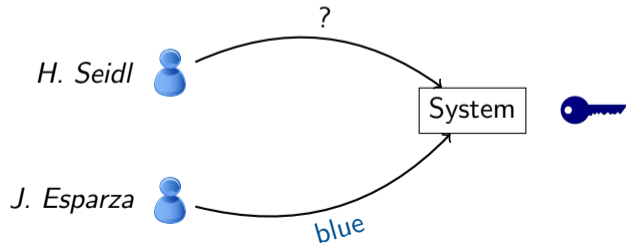
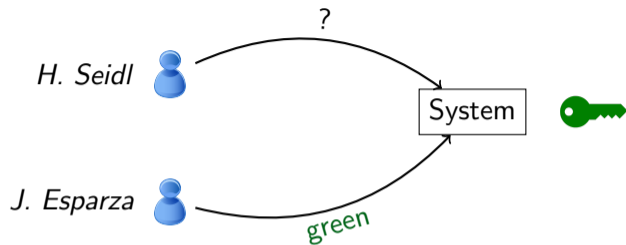


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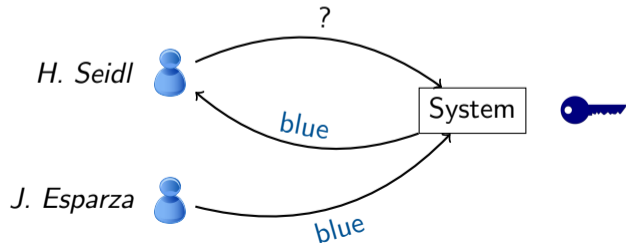
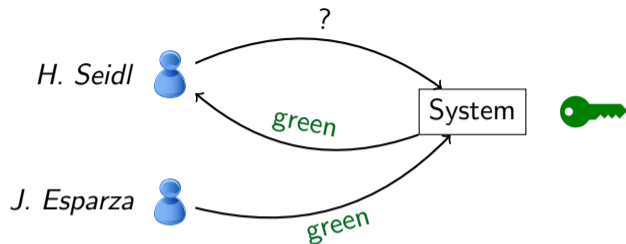
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## Stubborn Agents

Behavior does not depend on secret information.

# Agent Models

## Stubborn Agents

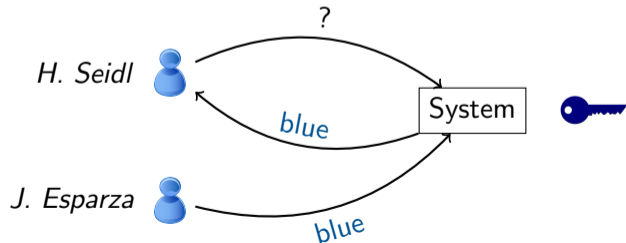
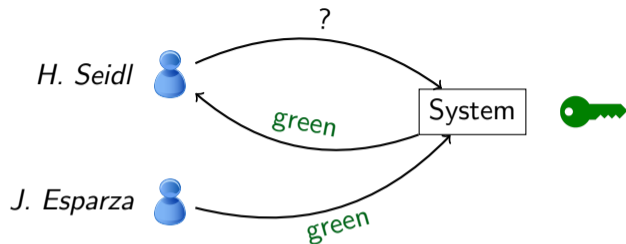
Behavior does not depend on secret information.

## Causal Agents

May change their behavior to leak information.

⇒ Causal agents may conspire against the system.

# Noninterference



# State of the Art

## Restricted Classes

Verification problem solved for restricted classes: Translation to  $\exists^*$ FOLTL<sup>1</sup>.

## General Case

Verification of Noninterference for general workflows is undecidable<sup>1</sup>.

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<sup>1</sup>Bernd Finkbeiner et al. “Verifying Security Policies in Multi-agent Workflows with Loops”. In: *Proceedings of the 2017 ACM SIGSAC Conference on Computer and Communications Security, CCS 2017, Dallas, TX, USA, October 30 - November 03, 2017*. 2017, pp. 633–645. DOI: 10.1145/3133956.3134080. URL: <http://doi.acm.org/10.1145/3133956.3134080>, p. 1.

# Simplifying the desired properties

Noninterference property consists of

Two copies of all relations  
Agent model  
Declassification  
No observable differences

Example: Declassification

$$\neg \text{Conflict}_1(x, p) \vee \neg \text{Conflict}_2(x, p)$$

Example: No observable differences

$$\mathbf{G} \wedge \forall \bar{z}. R_1(a, \bar{z}) \leftrightarrow R_2(a, \bar{z})$$

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Can be encoded into workflow

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Universal **G** property

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# Invariants

## Solution

Absence of Noninterference violations can be encoded into an invariant.

⇒ Prove workflows *safe* using invariants

## Section 2

# Proving Invariants



# Invariants

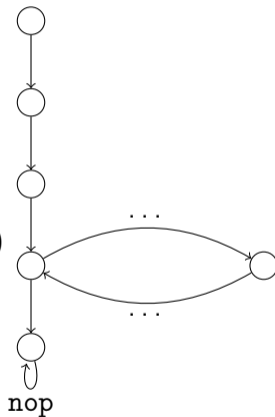
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**loop** { ... }



# Invariants

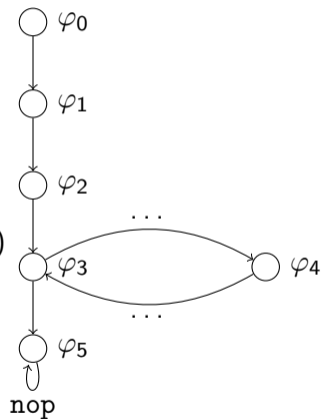
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# Invariants

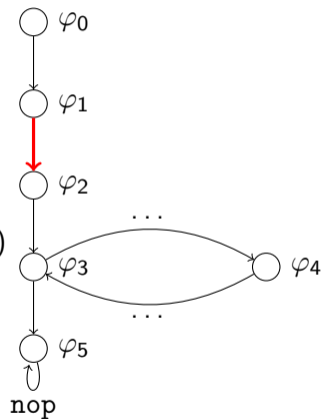
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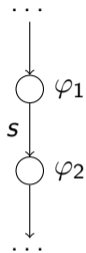
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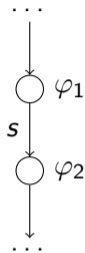
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# Proving Invariants inductive

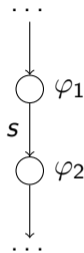


## Proving Invariants inductive



Does the statement respect the invariant?

## Proving Invariants inductive

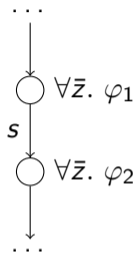


Does the statement respect the invariant?

Check if

$$\varphi_1 \rightarrow \text{WP}[[s]](\varphi_2)$$

## Proving Invariants inductive

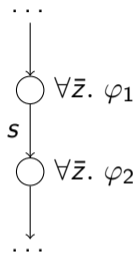


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## Proving Invariants inductive



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# Proving Invariants inductive

## How to check if an invariant holds

For an invariant  $\varphi$

- 1 Check inductiveness for all edges of the CFG
- 2 Check if the initial state implies  $\varphi_0$

( $\varphi$  is *inductive*)

( $\varphi$  is *safe*)

# Proving Invariants inductive

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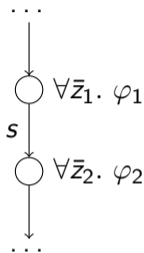
## Theorem (Correctness)

*For a given workflow  $w$  with and a universal invariant  $\varphi$ , it is decidable if  $\varphi$  is inductive and safe for  $w$ .*

## Section 3

# Inferring Inductive Invariants

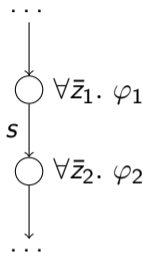
# Inferring Invariants



Can we strengthen if it does not?

$$\forall \bar{z}_1. \varphi_1 \rightarrow \text{WP}[[s]](\forall \bar{z}_2. \varphi_2) \quad \times$$

# Inferring Invariants



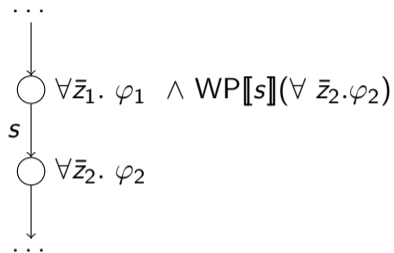
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# Inferring Invariants



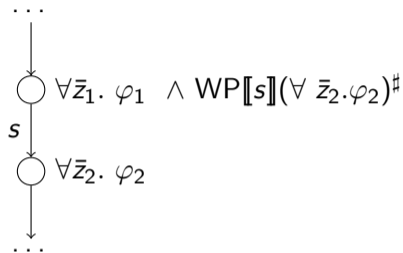
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# Inferring Invariants



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(and abstract existential quantifiers)

## Theorem (Inference)

*For a universal invariant  $\varphi$ , if fixpoint iteration terminates, we obtain an inductive universal invariant that implies  $\varphi$ .*



# Results

## Theorem (Inference)

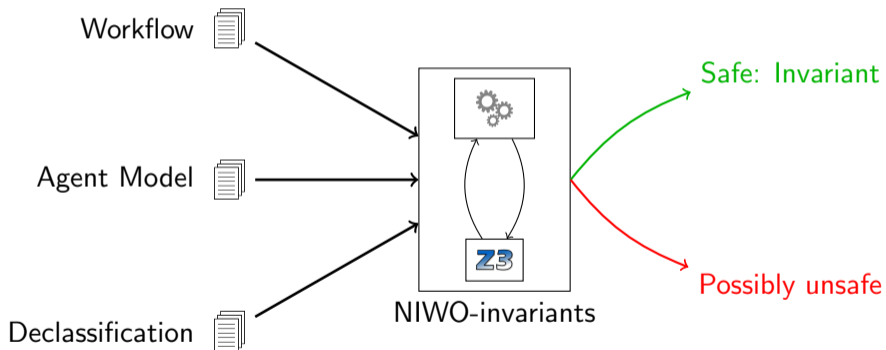
*For a universal invariant  $\varphi$ , if fixpoint iteration terminates, we obtain an inductive universal invariant that implies  $\varphi$ .*

## Corollary (Noninterference)

*For a given workflow  $w$ , if fixpoint iteration terminates, we obtain an inductive universal invariant that implies Noninterference for  $w$ .*

# Implementation

Meet *NIWO-invariants*, an automatic analyzer for **Non**interference in **Work**flows



# Implementation

Name	Size	Model	Result	Time
Conference_linear	4	stubborn	safe	338 ms
Conference_linear	4	causal	unsafe	1537 ms
Conference_linear_fixed	5	stubborn	safe	322 ms
Conference_linear_fixed	5	causal	safe	2352 ms
Conference_nonomitting	4	stubborn	safe	2170 ms
Conference_nonomitting	4	causal	unsafe	21488 ms
Conference_omitting	6	stubborn	safe	347 ms
Conference_omitting	6	causal	unsafe	2924 ms
Conference_omitting_fixed	7	stubborn	safe	1059 ms
Conference_omitting_fixed	7	causal	safe	5450 ms

# Will it terminate?

In general, termination not guaranteed.

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In general, termination not guaranteed.

## Termination Guarantee

- 1 Syntactic Fragment
- 2 Upper bound on # causal agents

# Contributions

- ① Transform Noninterference problem for workflows to invariant checking
- ② Introduced invariant verification and inference for general workflows
- ③ Built *NIWO-invariants*, an inferring invariant solver for Noninterference in general workflows